

# On Wavelength Asymmetry of Extinction-Ratio Improvement by Two-Wave Competition in ULSOAs

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Experiments have shown: the improvement of the extinction ratio (ER) by two-wave competition (TWC) exhibits a strong wavelength asymmetry. It "is a prerequisite for achieving an ER improvement, to set the CW beam to the long wavelength side of the signal" [1]. This asymmetry has qualitatively been attributed to the asymmetry of four-wave mixing (FWM). Here I shall check this hypothesis quantitatively on base of the theory presented in [1].

I consider copropagation of a signal and a CW wave with intensities  $S_s$  and  $S_{cw}$ , respectively, in the saturated SOA. The asymmetry of FWM is generally a result of the interferences between fast intraband contributions, represented by the gain saturation coefficient  $\varepsilon$ , and contributions from carrier population pulsations (CPP). In the appendix of pamphlet [2], I have already shown how the CPP contributions enter the evolution equation for the intensity ratio. Here, I rewrite these equations with an adapted notation.

$$\frac{\partial}{\partial z} \ln\left(\frac{S_s}{S_{cw}}\right) = q_s S_s - q_{cw} S_{cw}, \quad (1)$$

$$q_{s,cw} = g \left( \varepsilon \mp \frac{g' |\alpha_H| \lambda_0^2}{2\pi n_g (\lambda_{cw} - \lambda_s)} \right), \quad (2)$$

where the upper sign belongs to  $q_s$ .

The crucial points for the ER are the "zeros" of the signal bit sequence. Thus, I can confine to a case with  $S_s \ll S_{cw}$ . Thus, we can neglect the signal intensity on the r.h.s. of Eq. (1). Furthermore, saturation conditions require  $S_s + S_{cw} \approx S_{cw} = S_{sat}$ . Thus, we can approximate the cw intensity

by the saturation intensity, yielding

$$\frac{\partial}{\partial z} \ln\left(\frac{S_s}{S_{sat}}\right) = -q_{cw} S_{sat}, \quad (3)$$

Obviously, the quantity  $q_{cw}$  governs the decay of the signal intensity. The right hand side is constant, hence the solution is

$$S_s(z) \sim \exp(-z/L_s) \quad (4)$$

with the decay length

$$L_s = \frac{L_{TWC}}{1 + \Delta_{asym}/(\lambda_{cw} - \lambda_s)}. \quad (5)$$

Here  $L_{TWC}$  is the large-detuning limit of the characteristic decay length as given by formula (13) of our paper [1], and

$$\Delta_{asym} = \frac{g' |\alpha_H| \lambda_0^2}{2\pi n_g \varepsilon} \quad (6)$$

is a critical detuning below which the wavelength asymmetry becomes essential. With the parameters of [1], it is  $\Delta_{asym} = 3.86$  nm.

The effectiveness of ER improvement increases with the inverse of the signal decay length  $L_s$ . Thus, without explicitly calculating the ER, the plot of  $L_{TWC}/L_s$  in Fig.1 allows a theoretical estimate how the ER improvement should depend on the detuning. Indeed, it is quite similar to Fig.8 (a) of [1]. Of course, the agreement is not complete because the approximations hold only in the very last part of the SOA and the parameters are only estimates.

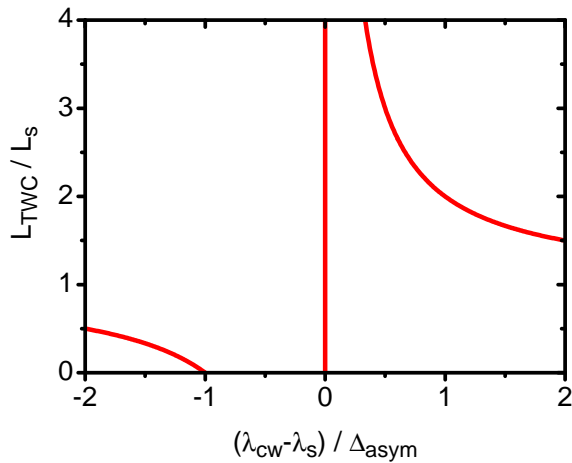


Fig.1: *Plot of the inverse decay length versus wavelength detuning.*

### Conclusion

The basic features of the measured wavelength asymmetry of the ER improvement by TWC are well described by the theory developed in [1].

### References

- [1] Gero Bramann, Hans-Jürgen Wünsche, Ulrike Busolt, Christian Schmidt, Michael Schlak, Bernd Sartorius, and Hans-Peter Nolting, "Two-Wave Competition in Ultra Long Semiconductor Optical Amplifiers", to appear in IEEE Journal Quantum Electronics, October 2005
- [2] H.-J. Wünsche, "Notes on Two-Wave Competition by Four-Wave Mixing", <http://photonik.physik.huberlin.de/ede/pamphlets/twcnote.pdf>