

Learned Feedback Control Mechanisms for a Quantum System

Alexander Hentschel

12 August 2008

Acknowledgements:



- 1 Introduction to Quantum Information
 - Quantum Bits (Qubits)
 - Quantum Operations
- 2 Learning about Quantum Systems
 - Application: Gravitational Wave Detection
- 3 Comparison and Conclusions

Quantum Computation & Information

study of information processing tasks that can be accomplished using **quantum mechanical systems**

Quantum mechanical system: (usually) system containing only few particles

Possible encodings of information:

- energy level of electrons
- electron spin
- polarization of light

Introduction to Quantum Information

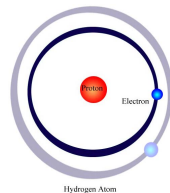
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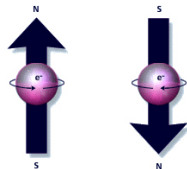
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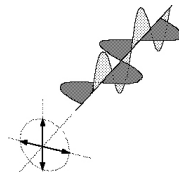
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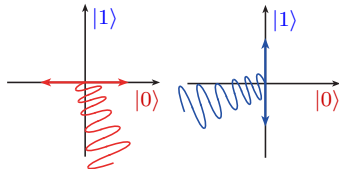
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Introduction to Quantum Information: Superposition

Encoding in polarization of light:

- logical 0: \leftrightarrow (horizontal polarization)
- logical 1: \updownarrow (vertical polarization)



Superposition

Probabilistic interpretation: (Bohr & Heisenberg, 1927)

Probability to measure qubit $|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle$ in

- state $|0\rangle$: $P(|0\rangle) = |\alpha|^2$
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State $|\tilde{\Psi}\rangle$ after measurement with

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mixture of $|0\rangle$ and $|1\rangle$:

example: $|\Psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$

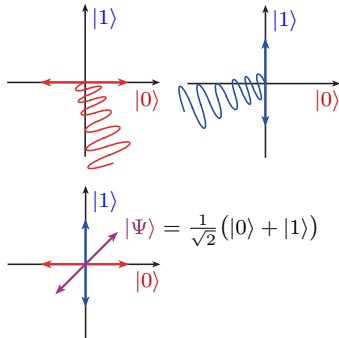
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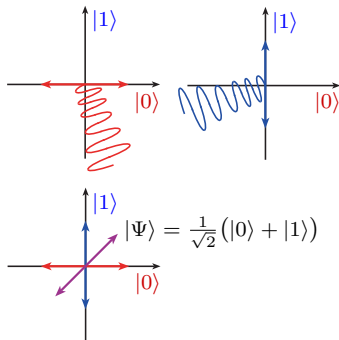
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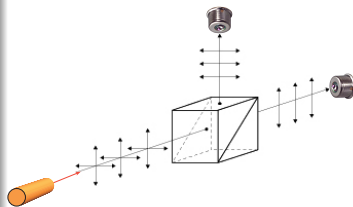
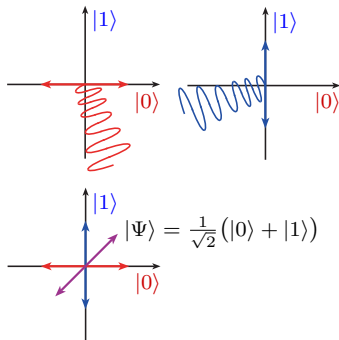
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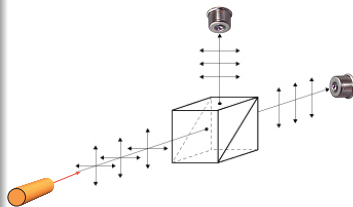
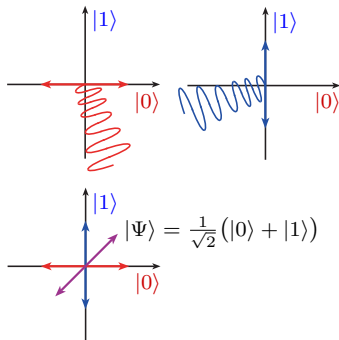
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Quantum Register $|\Psi\rangle$

with N qubits: 2^N classical states

- $|\Psi\rangle$ can be in any superposition of 2^N classical states

$$|\Psi\rangle = \alpha_0|0\rangle + \alpha_1|1\rangle + \dots + \alpha_{2^N-1}|2^N - 1\rangle$$

Quantum Operations

- Quantum Parallelism:
Operations act on *all* basis states of $|\Psi\rangle$
- Micro Reversibility:
in microsystem (usually) all processes reversible

Quantum operations = linear & invertible functions
(unitary matrices)

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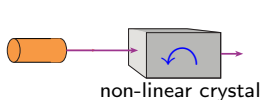
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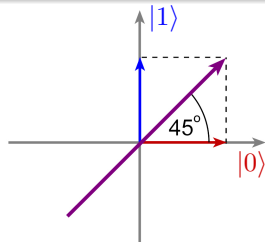
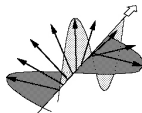
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rotates
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by fixed angle



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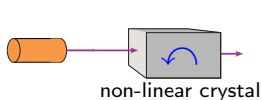
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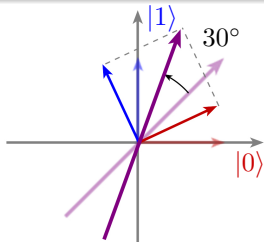
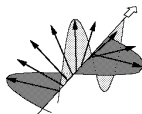
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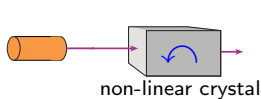
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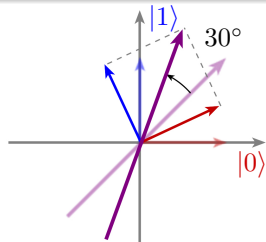
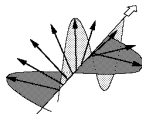
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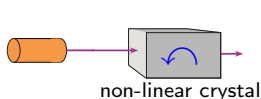
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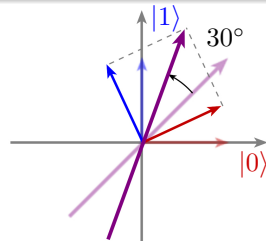
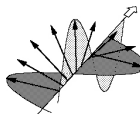
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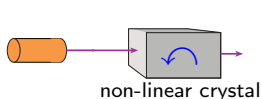
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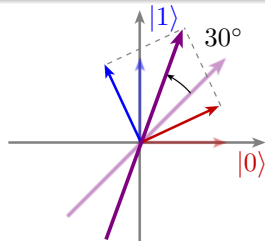
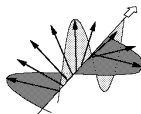
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Quantum register: $|\Psi\rangle = \alpha_0|0\rangle + \alpha_1|1\rangle + \alpha_2|2\rangle + \dots + \alpha_{2^N-1}|2^N - 1\rangle$

summary so far:

- reading out quantum register:
random outcome $|i\rangle$ with probability according to weight α_i
- after reading a quantum register:
information in $|\Psi\rangle$ destroyed (after measurement $|\Psi\rangle = |i\rangle$)

Question: Can one copy the state $|\Psi\rangle$ of a quantum register?

Answer: No!

No Cloning Theorem

There is no operation which can copy a quantum state $|\Psi\rangle$:

$$\text{COPY}\left(\underset{\substack{\uparrow \\ \text{quantum state}}}{|\Psi\rangle} \otimes \underset{\substack{\uparrow \\ \text{target register}}}{|\emptyset\rangle}\right) = |\Psi\rangle \otimes |\Psi\rangle$$

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Quantum Learning: Motivation

Artificial Intelligence

methods for classical
computation

- Bayesian Reasoning
- Neural Networks
- Evolutionary Algorithms
- \vdots

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provides extend computational model

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Quantum state: $|\Psi\rangle = \alpha_0|\psi_0\rangle + \dots + \alpha_{2^N-1}|\psi_{2^N-1}\rangle$

Full control over quantum system

Can prepare and measure $|\Psi\rangle$ repeatedly

- apply quantum tomography $|\Psi\rangle$:
similar to classical case, all system parameters known
- but: exponentially runtime in N

$|\Psi\rangle$

AI

Partial control over quantum system

Measurement perturbs $|\Psi\rangle$

- evolution of system is primarily driven by AI
- only partial information available

Implement learning on quantum level

- quantum parallelism: apply AI-algorithm to every $|\psi_i\rangle$

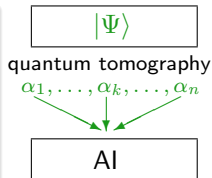
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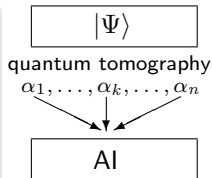
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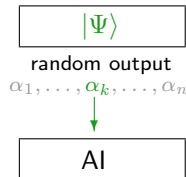
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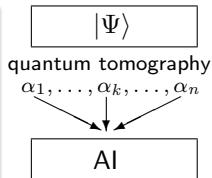
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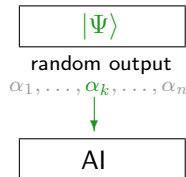
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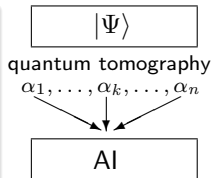
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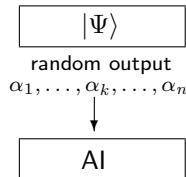
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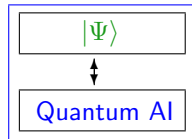
Measurement perturbs $|\Psi\rangle$

- evolution of system is primarily driven by AI
- only partial information available



Implement learning on quantum level

- quantum parallelism: apply AI-algorithm to every $|\psi_i\rangle$



Application: Gravitational Wave Detection

Possible application:

Detection of Gravitational Waves

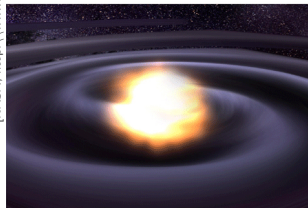
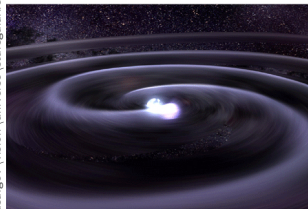
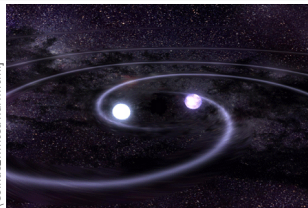
- move with speed of light
resource: time $\leftrightarrow N$ pulses
- extremely weak: $\sim 10^{-20}$
valuable resource: sensitivity

- LIGO, Washington, USA



- Detection: Mach-Zehnder Interferometer

[NASA, <http://www.nasa.gov/vision/universe/stargalaxies/collide/whitedwarf.html>]



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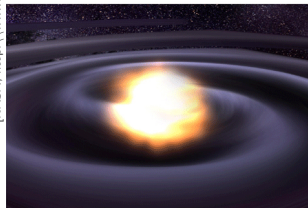
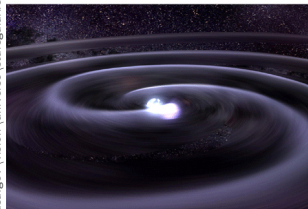
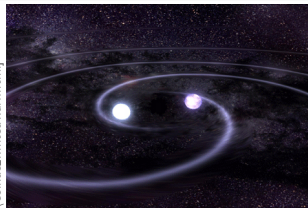
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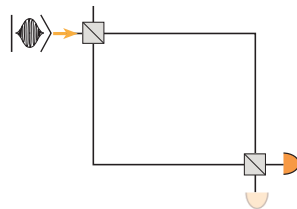
Application: Gravitational Wave Detection

- gravitational wave deforms optical path length

\Leftrightarrow phase shift Φ

- N photons: sensitivity $\Delta\Phi \sim \frac{1}{\sqrt{N}}$
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include controllable phase shifter φ
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Mach-Zehnder Interferometer



Beam Splitter



Phase Shifter



Detector

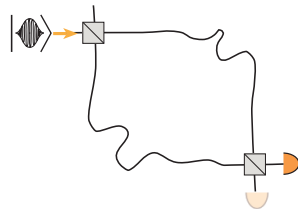
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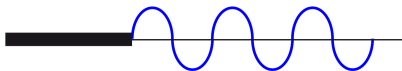
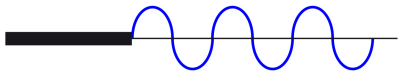
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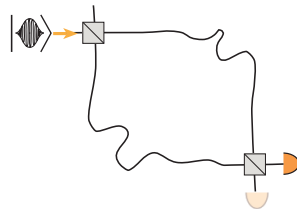


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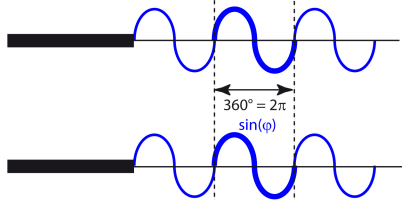
Phase Shifter



Detector

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No gravitational wave

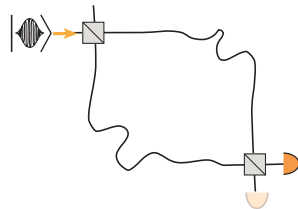


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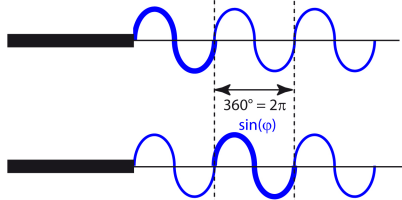
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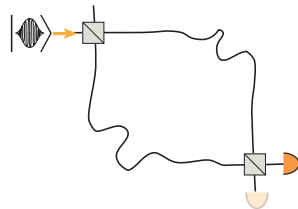


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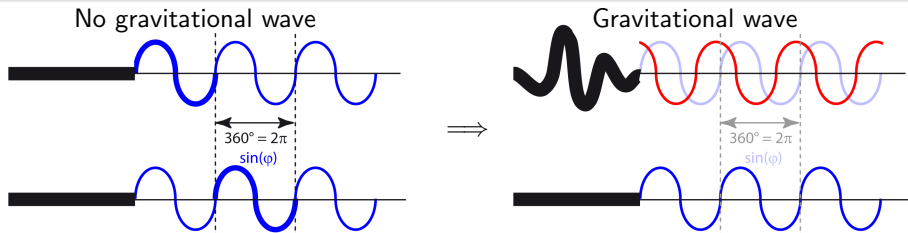


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■ Phase Shifter

◐ Detector

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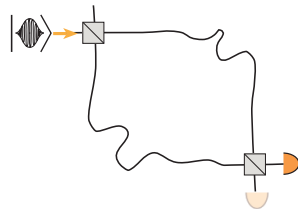


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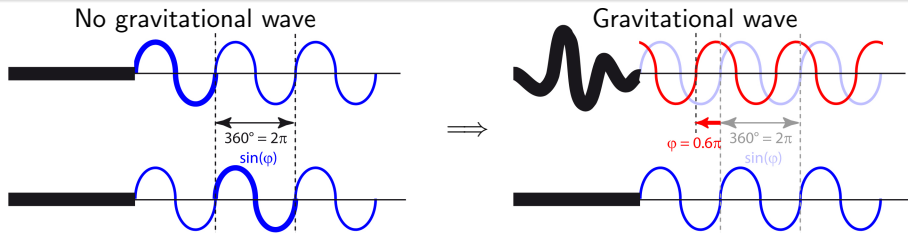


Phase Shifter



Detector

Application: Gravitational Wave Detection

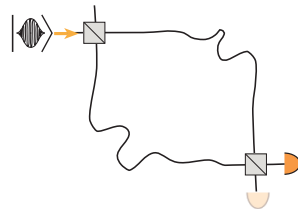


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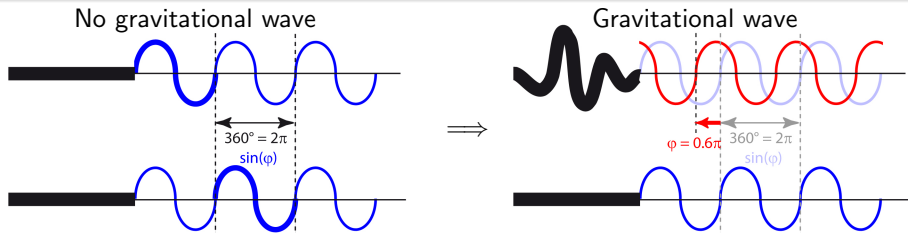


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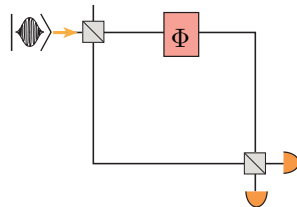


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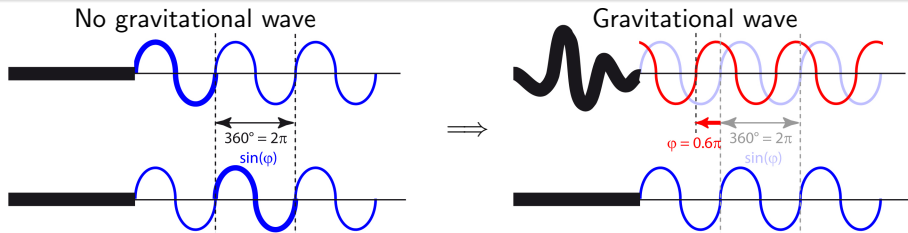


 Beam Splitter

 Phase Shifter

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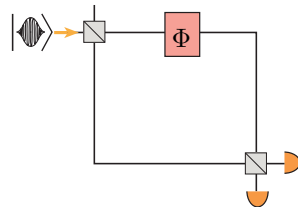


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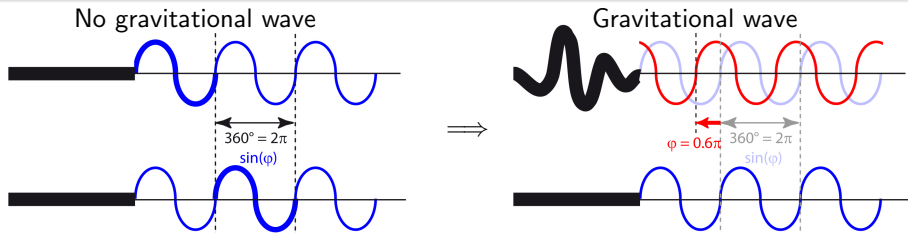


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Application: Gravitational Wave Detection



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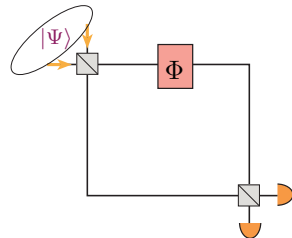
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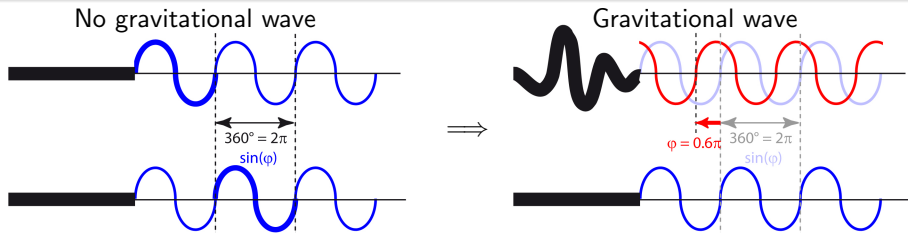


Phase Shifter



Detector

Application: Gravitational Wave Detection



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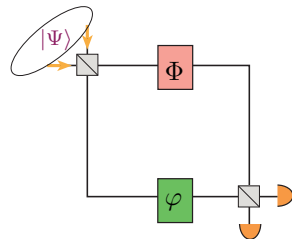
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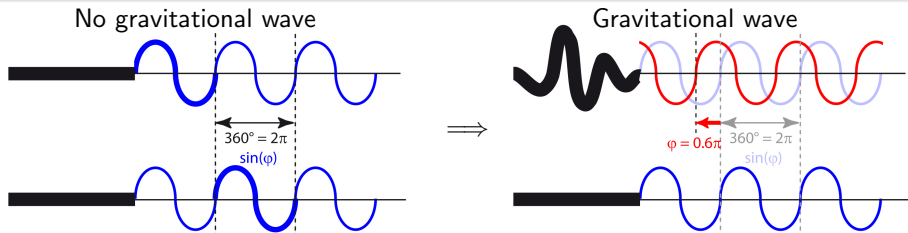


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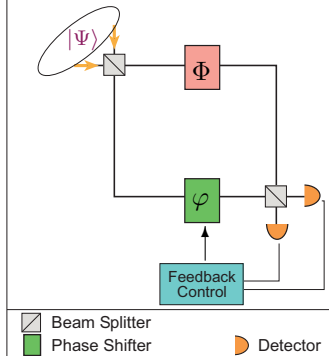
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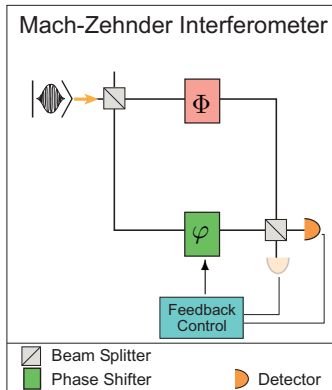
A simple feedback strategy

- input: N photons in horizontal arm
- tune φ until output:
only photons on horizontal arm

Disadvantages:

- bad sensitivity
 $\Delta\Phi \sim \frac{1}{\sqrt{N}}$
- to achieve sufficient sensitivity:
many photons required
 \Leftrightarrow measurement slow

Aim: feedback strategy with better sensitivity $\gtrsim \frac{1}{N}$



Feedback Algorithms

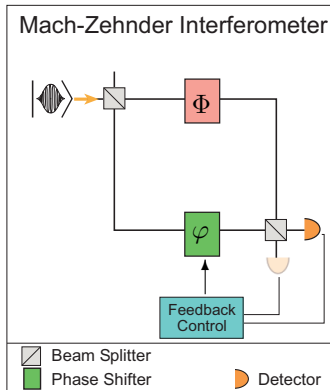
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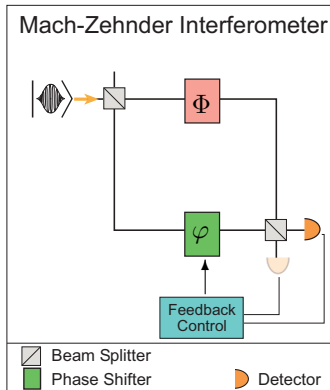


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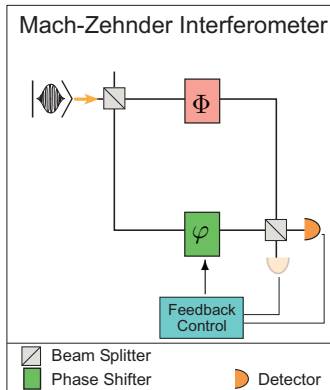
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Feedback Algorithms

A simple analogy of the learning problem

Guessing the number Φ rolled on a dice

- unknown parameter: Φ
- player can ask 3 questions $\varphi^{(0)}, \varphi^{(1)}, \varphi^{(2)}$
response: binary value
- after all 3 questions have been answered:
player gives estimate $\tilde{\Phi}$ for number rolled



Learning phase: Φ revealed *after game*

- feedback strategy
- reward gained at end of game

Gravitational Wave Detection

- unknown parameter: $\Phi \in [0, 2\pi]$
- action: choose $\varphi^{(i)} \in [0, 2\pi]$
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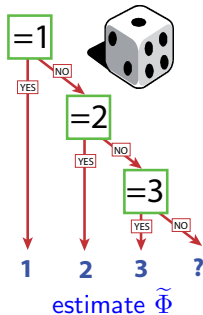
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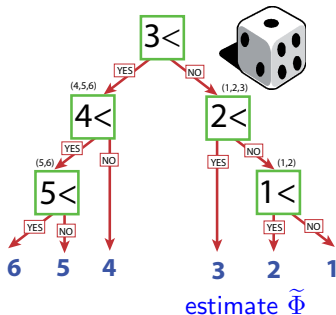
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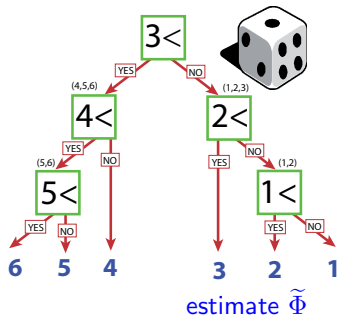
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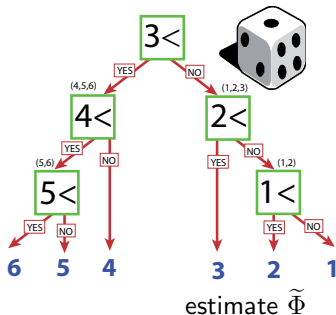
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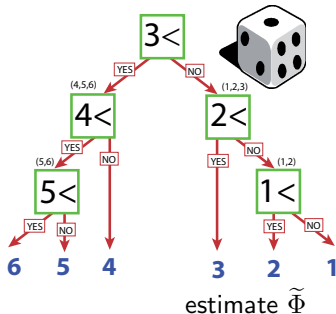
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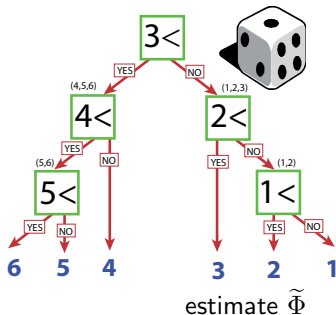
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Feedback Algorithms

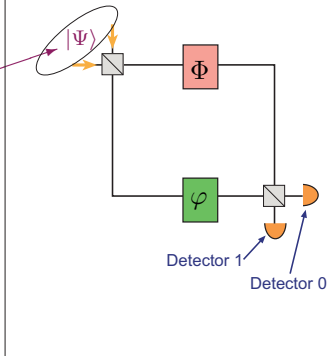
A high sensitivity feedback strategy

- input: fixed state $|\Psi\rangle$ of N entangled photons



- no prior information about Φ : select first phase $\varphi^{(0)}$ at random
- adjust phase $\varphi^{(0)} \rightarrow \varphi^{(1)}$ according to measurement outcome
- \vdots
- final phase estimates $\tilde{\Phi}$ determined by measurements

Mach-Zehnder Interferometer



Decision Tree Learning

evaluate fitness of decision tree with Bayes Theorem
vary decision tree using evolutionary algorithm

Feedback Algorithms

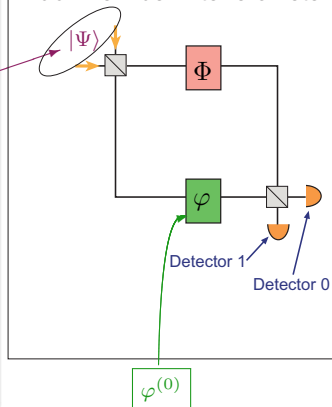
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Mach-Zehnder Interferometer



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evaluate fitness of decision tree with Bayes Theorem
vary decision tree using evolutionary algorithm

Feedback Algorithms

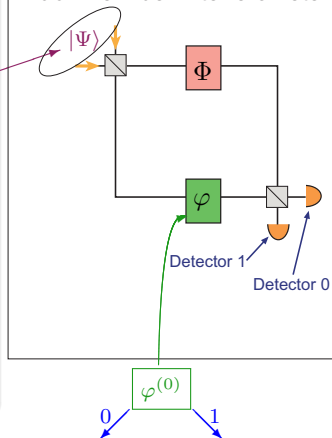
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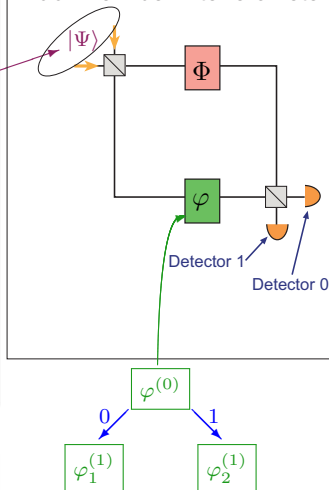
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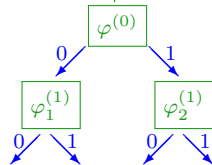
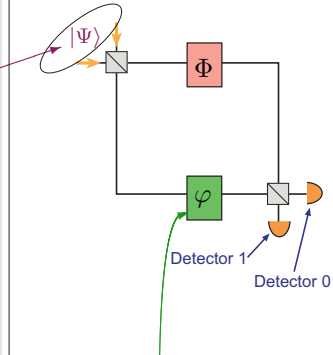
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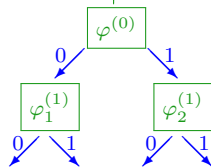
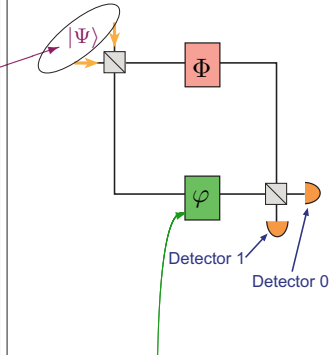
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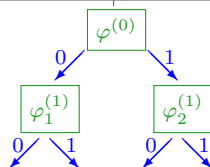
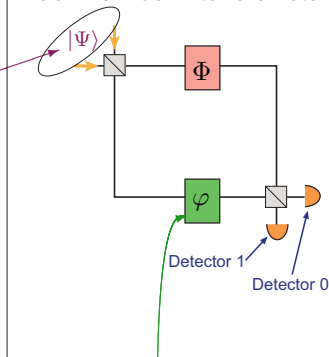
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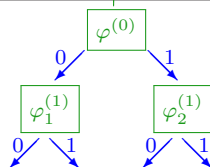
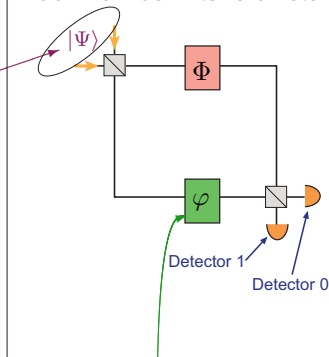


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Comments:

- **tree size exponential** in number of photons N

highest possible sensitivity $\sim \frac{1}{N}$

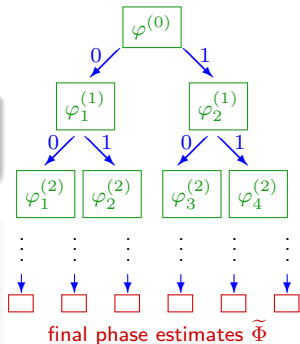
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without knowledge of specific noise process
- works for any prior distribution of phase Φ
- different input states $|\Psi\rangle$ possible
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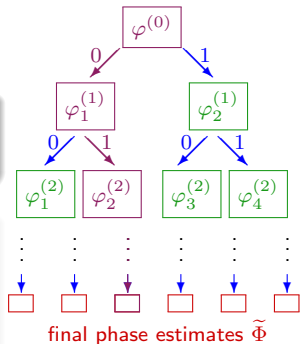
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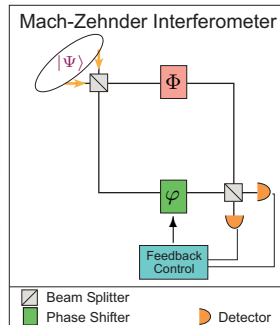
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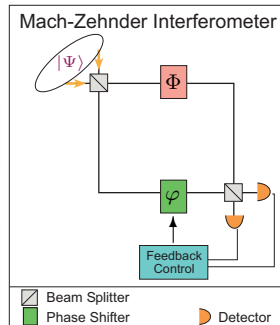
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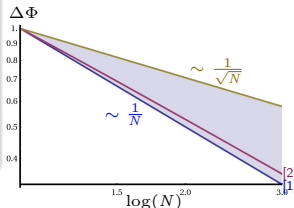
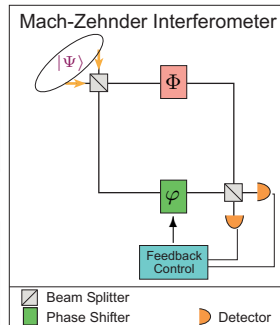
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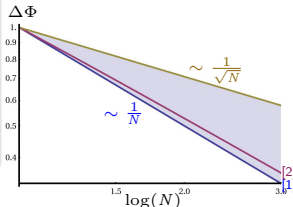
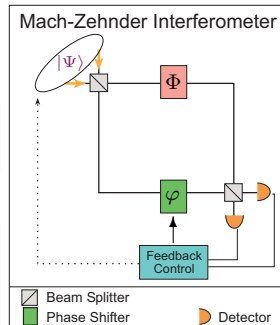
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Thank you for your attention.



Questions?

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- Searching an *unsorted* list
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- far from possible:
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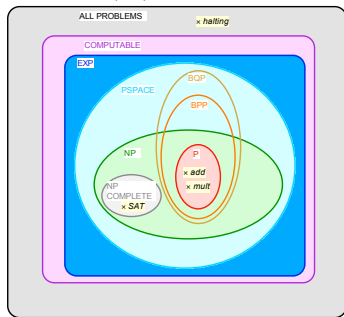
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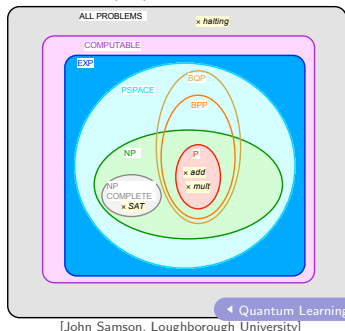
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